

1	(a)	$-3(x^2 - 4x) + 7$ or $-3\left(x^2 - 4x - \frac{7}{3}\right)$		4	M1 for factorising the expression to find b or $b = -3$ stated or shown clearly in answer.
		$-3\left[(x-2)^2 \dots\right]$ or $c = -2$ $-3\left[(x-2)^2 - 4\right] + 7$ or $-3\left[(x-2)^2 - 4 - \frac{7}{3}\right]$			M1 or for c shown clearly in answer.
		$-3(x-2)^2 + 12 + 7$ or $-3\left[(x-2)^2 - \frac{19}{3}\right]$			M1 fully correct method.
			$19 - 3(x-2)^2$		A1 for $19 - 3(x-2)^2$ oe
	(b)		(2, 19)	1	B1 ft dep on M1 in part (a) answer must follow answer from (a) if given
Total 5 marks					

Alternative mark scheme for 1

1	(a)	$a + bx^2 + 2bcx + bc^2$		4	M1 for multiplying out $a + b(x+c)^2$ to obtain $a + bx^2 + 2bcx + bc^2$ oe
		$b = -3$ or $2bc = 12$ or $a + bc^2 = 7$ oe			M1 for equating coefficients
		$b = -3$ and $c = -2$			M1 for correctly finding b and c
		$a = 19$	$19 - 3(x-2)^2$		A1 for $19 - 3(x-2)^2$ oe
	(b)		(2, 19)	1	B1 ft dep on M1 in part (a)
Total 5 marks					

2	a	$5 - (x \pm q)^2 + 9$ oe or $p - (x-3)^2$ oe or $p - q^2 + 2qx - x^2$ and one of $2q = 6$ or $p - q^2 = 5$			M1 may be seen in working eg $-(x-3)^2 - 9 - 5]$ or expanding $p - (x-q)^2$ correctly and equating one of the coefficient of x or the constant term
			$14 - (x-3)^2$	2	A1 fully correct SCB1 for $(x-3)^2 - 14$
	b	e.g. $(x-3)^2 = 14 - y$ [or $(y-3)^2 = 14 - x]$			M1 correct steps to isolate their bracket ft from (a) dep on expression in form $\pm p \pm (x-q)^2$
		$x = 3 \pm \sqrt{14-y}$ [or $y = 3 \pm \sqrt{14-x}$]			M1 complete method to find y in terms of x or x in terms of y . Condone + for \pm ft from (a) dep on expression in form $\pm p \pm (x-q)^2$
		$(f^{-1}(x) \Rightarrow) 3 - \sqrt{14-x}$			M1 for the correct inverse
					M1 method to solve $0 < 3 - \sqrt{14-x}$ or a lower bound of 5 clearly shown, eg $x > 5$ as part of the answer
			$5 < x \leq 14$	5	A1 cao
Total 7 marks					

3	b	E.g. $(x-5)^2 - 5^2 (+40)$ or $(x-5)^2 - 25 (+40)$ $(x^2 + 2ax + a^2 (+b^2))$ $2a = -10$ or $a = -5$		2	M1 for a correct first step or for equating coefficients
			$(x-5)^2 + 15$		A1 accept $a = -5$, $b = 15$ SC B1 for $(-x+5)^2 + 15$ or $(5-x)^2 + 15$

4	$(v =) 3t^2 - 9 \times 2t + 33$		5	M1	for differentiating at least 2 terms correctly
	$(a =) 3 \times 2t - '18'$ or $(t =) -\frac{-18}{2 \times 3} (= \frac{18}{6})$	$(v =) 3[(t-3)^2 - (3)^2] (+33)$ or $(v =) 3[(t-3)^2 - (3)^2 + 11]$		M1	dep fit must be a two term linear equation or for the use of $(t =) -\frac{b}{2a}$ or for a correct first step for completing the square on at least a two term quadratic
	$6t - 18 = 0$ or $t = 3$	$(v =) 3[(t-3)^2 - (3)^2] + 33$ or $(v =) 3[(t-3)^2 - (3)^2 + 11]$		M1	dep on at least M2 for equating their acceleration to 0 or for a correct method for completing the square on at least a two term quadratic
	$3 \times '3'^2 - 18 \times '3' + 33$	$(v =) 3(t-3)^2 + 6$ or $(v =) 3[(t-3)^2 + 2]$		M1	dep on at least M2 for substituting their t into v or for a seeing a correct simplified expression after completing the square
			6	A1	
Total 5 marks					

5	(a)	$2(x^2 - 6x) + 3$ or $2(x^2 - 6x + \frac{3}{2})$	3	M1	or for one of a , b or c correct OR expanding $a(x^2 + 2bx + b^2) + c$
		$2[(x-3)^2 - 9] + 3$ or $2[(x-3)^2 - 3^2 + \frac{3}{2}]$ oe		M1	or for two of a , b or c correct OR $-12 = 2ab$ or $3 = ab^2 + c$
				A1	accept $a = 2$, $b = -3$, $c = -15$

6		$-q(x^2 - \frac{12}{q}x) + q$ or $-q(x^2 - \frac{12}{q}x - \frac{q}{q})$ oe	4	M1	for a correct factorisation of the expression or $b = q$ (must be stated)
		$-q[x - \frac{12}{2q}]^2 \dots$ oe or $-q[x - \frac{6}{q}]^2 \dots$ oe		M1	for starting the correct process to complete the square
	E.g. $-q(x - \frac{6}{q})^2 + \frac{36}{q} + q$ oe or $-q(x - \frac{12}{2q})^2 + \frac{144q}{4q^2} + q$ oe			M1	for a complete process of completing the square. (Does not need to be simplified)
		$a = \frac{36}{q} + q$ $b = q$ $c = \frac{6}{q}$		A1	oe a and c must come from a correct process of completing the square. (Does not need to be simplified)
Total 4 marks					

6	ALT	$a - bx^2 + 2bcx - bc^2$ oe or $-bx^2 + 2bcx - bc^2 + a$ oe or $b = q$	4	M1	for correctly multiplying out $a - b(x-c)^2$
		$2bc = 12$ or $a - bc^2 = q$ oe		M1	for correctly equating coefficients
		$c = \frac{12}{2q}$ or $a = q(\frac{12}{2q})^2 + q$ or $c = \frac{6}{q}$ or $a = q(\frac{6}{q})^2 + q$		M1	for correctly finding a or c (Does not need to be simplified)
		$a = \frac{36}{q} + q$ $b = q$ $c = \frac{6}{q}$		A1	oe (Does not need to be simplified)
Total 4 marks					

7	(b)	$3(x^2 + 4x) + 19$ and $3[(x+2)^2 - 2^2] + 19$ or $3\left(x^2 + 4x + \frac{19}{3}\right)$ and $3\left((x+2)^2 - 2^2 + \frac{19}{3}\right)$ or $a = 3$ and $2ab = 12$ oe and $b^2a + c = 19$ oe or $a = 3$ and $b = \frac{12}{2 \times 3}$ oe and $c = -\frac{12^2}{4 \times 3} + 19$ oe			M1 for correctly taking out a factor of 3 and correctly completing the square or for equating coefficients by expanding $a(x+b)^2 + c = ax^2 + 2abx + b^2a + c$ or for equating coefficients by using $ax^2 + bx + c = a\left(x + \frac{b}{2a}\right)^2 - \frac{b^2}{4a} + c$
			$3(x+2)^2 + 7$		A1 accept $a = 3, b = 2, c = 7$

8	(a)	$7 - 3(x^2 - 4x)$		3	M1 or for one of a, b or c correct
		$7 - 3[(x-2)^2 - 4]$			M1 or for two of a, b or c correct
			$19 - 3(x-2)^2$		A1
	(b)		(2, 19)	1	B1 ft their expression
					Total 4 marks

9	(c)	$5(x^2 - 4x)$ or $5(x^2 - 4x)$ or $5(x-2)^2$...		3	M1
		$5[(x-2)^2 - (-2)^2]$ or $5[(x-2)^2 - (-2)^2]$ or $5(x-2)^2 - 20$ or $5\left[(x-2)^2 + \frac{3}{5}\right]$			M1 $(-2)^2$ can be 2^2 or 4 or $\left(\pm\frac{4}{2}\right)^2$
		Correct answer scores full marks (unless from obvious incorrect working)	$5(x-2)^2 + 3$		A1

Alternative mark scheme for 9c

	$ax^2 - 2abx + ab^2 + c$		3	M1 for multiplying out $a(x-b)^2 + c$ to obtain $ax^2 - 2abx + ab^2 + c$ oe
	2 of: $a = 5$ $2ab = 20$ oe $ab^2 + c = 23$ oe			M1 for equating coefficients and making 2 correct statements
		$5(x-2)^2 + 3$		A1

10	$3(x^2 - 2x)$ or $3(x^2 - 2x + \dots)$ oe or		3	M1 (where is any number or no number)
	$3(x-1)^2$ or $3[(x-1)^2 \dots]$ oe			M1 (where is any number or no number)
	Correct answer scores full marks (unless from obvious incorrect working)	$3(x-1)^2 + 2$		A1 (if student continues to solve a quadratic equation, ISW)
				Total 3 marks

Alternative mark scheme for 10

10	$ax^2 - 2abx + ab^2 + c$		3	M1 for multiplying out $a(x-b)^2 + c$ to obtain $ax^2 - 2abx + ab^2 + c$ oe
	Any 2 of the following: $a = 3$ or $2ab = 6$ or $ab^2 + c = 5$ oe			M1 for equating coefficients with any 2 of $a = 3$ or $2ab = 6$ or $ab^2 + c = 5$ oe seen
	Correct answer scores full marks (unless from obvious incorrect working)	$3(x-1)^2 + 2$		A1 (if student continues to solve a quadratic equation, ISW)
				Total 3 marks